

## TÓRTINCHI TARTIBLI TENGLAMA UCHUN BIR CHEGARAVIY MASALANING YECHILISHI

**E.Satullaev**

Berdaq nomidagi Qoraqalpoq davlat universiteti, Nukus,

Qoraqalpogʻiston

E-mail: [antiterror8128@gmail.com](mailto:antiterror8128@gmail.com)

**Annotatsiya:** Maqolada tórtinchi tartibli tartibli xususiy xosilali differencial tenglama uchun tórtburchakli sohada bir aralash-chegaraviy masala kórib chiqildi. Masala yechimining mavjudligi va yagonaligi kórsatildi. Masala yechimini topish uchun ózgaruvchilarni ajratish usuli qóllanildi. Masala yechimi xususiy funkciyalar bóyicha qatorga yigib topildi. Yechimning yagonaligi ortonormallangan sistemaning tóliqligidan foydalanib kórsatildi.

**Kalit sózlar:** boshlangʻich-chegaraviy masala, ózgaruvchilarni ajratish usuli, yechimning yagonaligi, mavjudligi, xususiy qiymatlar va funkciyalar.

**Kirish:** Geofizikaning, okeanologiyaning birqancha masalalari, texnikada kriogen suyuqliklarni shuningdek, stratificirlangan suyuqliklarni foydalanish masalalari, elastiklik teoriyasining masalalari, bir jinsli sterejenning yoki balkaning tebranish tenglamasi tórtinchi tartibli xususiy xosilali differencial tenglamalar uchun qóyilgan chegaraviy, boshlangʻich-chegaraviy masalalarni yechishga keltiriladi.

Tórtburchakli sohada tórtinchi tartibli xususiy xosilali differencial tenglamalar uchun qóyilgan masalalar M.M. Smirnovning[10], T.D. Djuraevning va A. Sopuevning[6], K.B. Sabitovning [8-9], A.Berdishevning va B.J. Kadirkulovning[4], Ya. Megralievning [7], D. Amanovning[1-2], T. Yuldashovning[12], A.Urinovning[11], Yu. Apakovning[3] va h.k. ishlarida qaralgan.

[10] monografiyasida tórtinchi tartibli xususiy xosilali differencial tenglamalarning tóliq klassifikatsiyasi va u tenglamalar uchun qóyilgan masalalarni yechish qaralgan. [5] ishda tórtinchi tartibli tenglamalar uchun bir chegaraviy masala qaralgan.

### **Masalaning qóyilishi**

$\Omega = \{(x, y): 0 < x < p, 0 < t < \beta\}$  sohada

$$U_{ttt} + U_{xxxx} = 0 \quad (1)$$

tenglamani kóramiz, bu yerda  $p, T \in \mathbb{R}$ .

**Masala 1.**  $\Omega$  sohada (1) tenglamaning quyidagi

$$u|_{x=0} = 0, u|_{x=p} = 0, u_{xx}|_{x=0} = 0, u_{xx}|_{x=p} = 0, \quad 0 \leq x \leq p \quad (2)$$

$$u|_{t=0} = \varphi(x) \quad u|_{t=\beta} = \psi(x) \quad u_t|_{t=\beta} = \eta(x) \quad 0 \leq t \leq \beta \quad (3)$$

chegaraviy shartlarni qanoatlandiradigan

$$u(x, y) \in C_{x,t}^{4,3}(\Omega) \cap C_{x,t}^{2,1}(\bar{\Omega})$$

sinfga tegishli yechimini izlaymiz, bunda  $\psi_i(x), i = \overline{1,3}$  yetarlicha silliq funkciyalar va

$$\begin{aligned} \varphi(0) = \varphi(p) = \varphi''(0) = \varphi''(p) = 0, \\ \psi(0) = \psi(p) = \psi''(0) = \psi''(p) = 0, \quad \eta(0) = \eta(p) = 0, \end{aligned} \quad (4)$$

## 2. Masala yechimining mavjudligi

Masalaning yechimga ega ekanligini isbotlaymiz: (1) tenglamaning (2) chegaraviy shartlarni qanoatlandiradigan trivial blmagan yechimini

$$u(x, y) = X(x)U(t). \quad (5)$$

krinishida izlaymiz.

(5) ni (1) tenglamaga qyish va zgaruvchilarni ajratish orqali  $X(x)$  va  $U(t)$  funkciyalar uchun quyidagi differencial tenglamalarga ega blamiz:

$$X^{(4)}(x) - \lambda^4 X(x) = 0 \quad (6)$$

$$U_k^{(3)}(t) + \lambda_k^4 U_k(t) = 0 \quad (7)$$

bunda  $\lambda^4$  zgarmas.

(2) chegaraviy shartlarni hisobga olgan holda (6) tenglama uchun quyidagi masalaga ega blamiz:

$$\begin{cases} X^{(4)}(x) - \lambda^4 X(x) = 0 \\ X(0) = X(p) = X''(0) = X''(p) = 0 \end{cases} \quad (8)$$

(8) masala trivial blmagan yechimga ega bladi, bunda

$$\lambda_k^4 = \left( \frac{\pi k}{p} \right)^4, \quad n = 1, 2, 3, \dots$$

Bu sonlar (8) masalaning xususiy qiymatlari deyiladi va ularga mos keladigan normalangan xususiy funkciyalar quyidagi krinishda bladi:

$$X_k(x) = \sqrt{\frac{2}{p}} \sin \frac{\pi k}{p} x. \quad (9)$$

(7) ning bir jinsli yechimi

$$U_k(t) = a_k e^{-\nu_k t} + e^{\frac{1}{2} \nu_k t} \left( b_k \cos \left( \frac{\sqrt{3}}{2} \nu_k t \right) + c_k \sin \left( \frac{\sqrt{3}}{2} \nu_k t \right) \right)$$

kórinishida bóladi, bunda  $\nu_k = \sqrt[3]{\lambda_k^4} = \left(\frac{\pi k}{p}\right)^{4/3}$ ,  $n \in N$  va  $a_k, b_k, c_k$  - hozircha nomalum ózgarmaslar. Ózgarmaslarni variatsiyalash usulidan foydalanib yechimni

$$U_k(t) = a_k(t)e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left( b_k(t) \cos\left(\frac{\sqrt{3}}{2}\nu_k t\right) + c_k(t) \sin\left(\frac{\sqrt{3}}{2}\nu_k t\right) \right), \quad (10)$$

kórinishida izlaymiz.

(1) tenglamaning umumiy yechimi

$$u(x, y) = \sqrt{\frac{2}{p}} \sum_{k=1}^{\infty} \left( a_k(t)e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left( b_k(t) \cos\left(\frac{\sqrt{3}}{2}\nu_k t\right) + c_k(t) \sin\left(\frac{\sqrt{3}}{2}\nu_k t\right) \right) \right) \sin \frac{\pi k}{p} x$$

qator kórinishida bóladi.  $a_k(t), b_k(t), c_k(t)$  funkciyalarni topish uchun (10) tenglikdan 3 marta xosila olib (1) tenglamaga qóyamiz va quyidagi tenglamalar sistemasiga ega bólamiz:

$$\begin{aligned} & a'_k(t)e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left[ b'_k(t) \cos\frac{\sqrt{3}}{2}\nu_k t + c'_k(t) \sin\frac{\sqrt{3}}{2}\nu_k t \right] = 0 \\ & -a'_k(t)e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left( \left[ \frac{1}{2} \cos\frac{\sqrt{3}}{2}\nu_k t - \frac{\sqrt{3}}{2} \sin\frac{\sqrt{3}}{2}\nu_k t \right] b'_k(t) + \right. \\ & \left. + \left[ \frac{1}{2} \sin\frac{\sqrt{3}}{2}\nu_k t + \frac{\sqrt{3}}{2} \cos\frac{\sqrt{3}}{2}\nu_k t \right] c'_k(t) \right) = 0 \\ & a'_k(t)e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left( \left[ -\frac{1}{2} \cos\frac{\sqrt{3}}{2}\nu_k t - \frac{\sqrt{3}}{2} \sin\frac{\sqrt{3}}{2}\nu_k t \right] b'_k(t) + \right. \\ & \left. + \left[ -\frac{1}{2} \sin\frac{\sqrt{3}}{2}\nu_k t + \frac{\sqrt{3}}{2} \cos\frac{\sqrt{3}}{2}\nu_k t \right] c'_k(t) \right) = 0 \end{aligned}$$

Bu sistemani yechish orqali  $a'_k(t), b'_k(t), c'_k(t)$  lar uchun

$$a'_k(t) = b'_k(t) = c'_k(t) = 0$$

tengliklarga ega bólamiz. Endi bularni integrallash orqali  $a_k(t), b_k(t), c_k(t)$  funkciyalarni topamiz:

$$a_k(t) = a_k \quad b_k(t) = b_k \quad c_k(t) = c_k$$

Bu topilganlarni (10) tenglikka qóyish orqali

$$U_k(t) = a_k e^{-\nu_k t} + e^{\frac{1}{2}\nu_k t} \left( b_k \cos\left(\frac{\sqrt{3}}{2}\nu_k t\right) + c_k \sin\left(\frac{\sqrt{3}}{2}\nu_k t\right) \right), \quad (12)$$

yechimga ega bólamiz. Bunda  $a_k, b_k, c_k$  -hozircha nomalum ózgarmaslar.  $a_k, b_k, c_k$  ózgarmaslarni topish uchun (3) shartlardan foydalanamiz. (3) shartlardan

$$U_k(0) = \varphi_k, U_k(\beta) = \psi_k, U_k'(\beta) = \eta_k$$

kelib chiqadi, bu yerda

$$\begin{aligned} \varphi(x) &= \sqrt{\frac{2}{p}} \sum_{k=1}^{\infty} \varphi_k \sin \frac{\pi k}{p} x, \psi(x) = \sqrt{\frac{2}{p}} \sum_{k=1}^{\infty} \psi_k \sin \frac{\pi k}{p} x, \eta(x) = \sqrt{\frac{2}{p}} \sum_{k=1}^{\infty} \eta_k \sin \frac{\pi k}{p} x, \\ \varphi_k &= \sqrt{\frac{2}{p}} \int_0^p \varphi(\xi) \sin \frac{\pi k}{p} \xi d\xi, \psi_k = \sqrt{\frac{2}{p}} \int_0^p \psi(\xi) \sin \frac{\pi k}{p} \xi d\xi, \eta_k = \sqrt{\frac{2}{p}} \int_0^p \eta(\xi) \sin \frac{\pi k}{p} \xi d\xi \end{aligned} \quad (1)$$

(10) funkciyani (13) shartlarga qóyib

$$\begin{cases} a_k + b_k = \varphi_k, \\ a_k e^{-v_k \beta} + e^{\frac{1}{2} v_k \beta} \left( b_k \cos \left( \frac{\sqrt{3}}{2} v_k \beta \right) + c_k \sin \left( \frac{\sqrt{3}}{2} v_k \beta \right) \right) = \psi_k \\ -v_k e^{-v_k \beta} a_k + v_k e^{\frac{1}{2} v_k \beta} \cos \left( \frac{\pi}{3} + \frac{\sqrt{3}}{2} v_k \beta \right) b_k + v_k e^{\frac{1}{2} v_k \beta} \sin \left( \frac{\pi}{3} + \frac{\sqrt{3}}{2} v_k \beta \right) c_k = \eta_k \end{cases} \quad (14)$$

tenglamalar sistemasiga ega bólamiz.

(14) sistemaning determinanti

$$\Delta = \frac{\sqrt{3}}{2} v_k e^{v_k \beta} - \sqrt{3} v_k e^{-\frac{1}{2} v_k \beta} \sin \left( \frac{\pi}{6} + \frac{\sqrt{3}}{2} v_k \beta \right)$$

bóladi. Bu determinant qiymati 0 dan katta bóladi.

Unda (14) sistemaning yechimi

$$\begin{aligned} a_k &= \frac{1}{\Delta} \left[ \varphi_k \frac{\sqrt{3}}{2} v_k e^{v_k \beta} - \psi_k v_k e^{\frac{1}{2} v_k \beta} \sin \left( \frac{\pi}{3} + \frac{\sqrt{3}}{2} v_k \beta \right) + \eta_k e^{\frac{1}{2} v_k \beta} \sin \left( \frac{\sqrt{3}}{2} v_k \beta \right) \right], \\ b_k &= \frac{1}{\Delta} \left[ -\varphi_k \sqrt{3} v_k e^{-\frac{1}{2} v_k \beta} \sin \left( \frac{\pi}{6} + \frac{\sqrt{3}}{2} v_k \beta \right) + \right. \\ &\quad \left. + \psi_k v_k e^{\frac{1}{2} v_k \beta} \sin \left( \frac{\pi}{3} + \frac{\sqrt{3}}{2} v_k \beta \right) - \eta_k e^{\frac{1}{2} v_k \beta} \sin \left( \frac{\sqrt{3}}{2} v_k \beta \right) \right] \\ c_k &= \frac{1}{\Delta} \left[ \varphi_k \sqrt{3} v_k e^{-\frac{1}{2} v_k \beta} \cos \left( \frac{\pi}{6} + \frac{\sqrt{3}}{2} v_k \beta \right) - \right. \\ &\quad \left. - \psi_k \left( v_k e^{\frac{1}{2} v_k \beta} \cos \left( \frac{\pi}{3} + \frac{\sqrt{3}}{2} v_k \beta \right) + v_k e^{-v_k \beta} \right) + \eta_k \left( e^{\frac{1}{2} v_k \beta} \cos \left( \frac{\sqrt{3}}{2} v_k \beta \right) - e^{-v_k \beta} \right) \right] \end{aligned} \quad (15)$$

bóladi.

$a_k, b_k, c_k$  koefitsientlarning topilgan qiymatlarini (12) da órniga oborib qóyamiz. Demak (1) tenglamaning (2) va (3) shartlarni qanoatlandiradigan yechimi (12) kórinishida bóladi.  $a_k, b_k, c_k$  koefitsientlarini baholaymiz:

$$\begin{aligned} |a_k| &\leq \frac{C_1}{\Delta} \left[ |\varphi_k| \nu_k e^{\nu_k \beta} + |\psi_k| \nu_k e^{\frac{1}{2} \nu_k \beta} + |\eta_k| e^{\frac{1}{2} \nu_k \beta} \right] \\ |b_k| &\leq \frac{C_2}{\Delta} \left[ |\varphi_k| \nu_k e^{-\frac{1}{2} \nu_k \beta} + |\psi_k| \nu_k e^{\frac{1}{2} \nu_k \beta} + |\eta_k| e^{\frac{1}{2} \nu_k \beta} \right] \\ |c_k| &\leq \frac{C_3}{\Delta} \left[ |\varphi_k| \nu_k e^{-\frac{1}{2} \nu_k \beta} + |\psi_k| \nu_k e^{\frac{1}{2} \nu_k \beta} + |\eta_k| e^{\frac{1}{2} \nu_k \beta} \right]. \end{aligned} \quad (16)$$

$\varphi_k(x), \psi_k(x)$  larni 5 marta va  $\eta(x)$  ni 4 marta bólaklab integrallaymiz.

$$\varphi_k = \frac{1}{\lambda_k^5} \bar{\varphi}_k^{(5)}, \quad \bar{\varphi}_k^{(5)} = \sqrt{\frac{2}{p}} \int_0^p \varphi_k^{(5)}(x) \cos \lambda_k x dx,$$

$$\psi_k = \frac{1}{\lambda_k^5} \bar{\psi}_k^{(5)}, \quad \bar{\psi}_k^{(5)} = \sqrt{\frac{2}{p}} \int_0^p \psi_k^{(5)}(x) \cos \lambda_k x dx,$$

$$\eta_k = \frac{1}{\lambda_k^4} \bar{\eta}_k^{(4)}, \quad \bar{\eta}_k^{(4)} = \sqrt{\frac{2}{p}} \int_0^p \eta_k^{(4)}(x) \sin \lambda_k x dx,$$

bu yerda  $\varphi^{(2j)}(0) = \varphi^{(2j)}(p) = 0, j = 0, 1, 2, \psi^{(2j)}(0) = \psi^{(2j)}(p) = 0, j = 0, 1, 2,$

$\eta^{(2j)}(0) = \eta^{(2j)}(p) = 0, j = 0, 1,$

$\varphi_k, \psi_k, \eta_k$  larning bu qiymatlarini (16) tengsizlikning óng tarafiga qóyib

$$|\varphi_k| \leq M \frac{|\bar{\varphi}_k^{(5)}|}{k^5}, \quad |\psi_k| \leq M \frac{|\bar{\psi}_k^{(5)}|}{k^5}, \quad |\eta_k| \leq M \frac{|\bar{\eta}_k^{(4)}|}{k^4}, \quad (17)$$

$a_k, b_k, c_k$  uchun biz quyidagi baholashlarni yoza olamiz:

$$|a_k| \leq M \left( \frac{|\bar{\varphi}_k^{(5)}|}{k^5} + \frac{|\bar{\psi}_k^{(5)}|}{k^5} + \frac{|\bar{\eta}_k^{(4)}|}{k^5} \right),$$

$$|b_k| \leq M e^{-\nu_k \beta} \left( \frac{|\bar{\varphi}_k^{(5)}|}{k^5} + \frac{|\bar{\psi}_k^{(5)}|}{k^5} + \frac{|\bar{\eta}_k^{(4)}|}{k^5} \right),$$

$$|c_k| \leq M e^{-\nu_k \beta} \left( \frac{|\bar{\varphi}_k^{(5)}|}{k^5} + \frac{|\bar{\psi}_k^{(5)}|}{k^5} + \frac{|\bar{\eta}_k^{(4)}|}{k^5} \right)$$

(11) qatorni hadma-had t b6yicha 3 marta, x b6yicha 4 marta differenciallaymiz.

(11) qatorning va uning mos xosilalaridan tuzilgan qatorlarning  $\bar{\Omega}$  sohada teng 6lchovli yaqinlashuvchiligini k6rsatish kerak.

**1-teorema.** Eger  $\varphi(x), \psi(x) \in C^5[0, p]$ ,  $\eta(x) \in C^4[0, p]$ , hamda (4) maxsus shartlarni qanoatlandirsa, unda 1-masala yechimi bor va u (11) qator k6rinishida yoziladi.

**Isbot.** Agar (11) qator va uning  $u_{xxxx}, u_{ttt}$  xosilalari  $\bar{\Omega}$  sohada bir qiymatli aniqlansa, unda ushbu qator orqali berilgan  $u(x, y)$  funkciya 1 masala yechimi b6ladi.

(11) dan

$$|u(x, y)| \leq \sqrt{\frac{2}{p}} \sum_{n=1}^{\infty} (|a_k| + |b_k| e^{\nu_k \beta} + |c_k| e^{\nu_k \beta}) \quad (18)$$

kelib chiqadi. Unda (15) ni hisobga olgan holda (16) dan

$$|u(x, y)| \leq M \left( \sum_{n=1}^{\infty} \frac{|\bar{\varphi}_k^{(5)}|}{k^5} + \sum_{n=1}^{\infty} \frac{|\bar{\psi}_k^{(5)}|}{k^5} + \sum_{n=1}^{\infty} \frac{|\bar{\eta}_k^{(5)}|}{k^5} \right) < \infty$$

b6ladi.

$$u_{xxxx} = \sum_{n=1}^{\infty} \lambda_k^4 \left[ a_k e^{\nu_k y} + e^{-\frac{1}{2} \nu_k y} \left( b_k \cos \left( \frac{\sqrt{3}}{2} \nu_k y \right) + c_k \sin \left( \frac{\sqrt{3}}{2} \nu_k y \right) \right) \right] X_k(x)$$

$$|u_{xxxx}| \leq \sqrt{\frac{2}{p}} \sum_{n=1}^{\infty} \lambda_k^4 (|C_1| + |C_2| e^{\nu_k \beta} + |C_3| e^{\nu_k \beta}) \leq M \left( \sum_{n=1}^{\infty} \frac{|\bar{\varphi}_k^{(5)}|}{k} + \sum_{n=1}^{\infty} \frac{|\bar{\psi}_k^{(5)}|}{k} + \sum_{n=1}^{\infty} \frac{|\bar{\eta}_k^{(5)}|}{k} \right)$$

Bu tengsizlikning 6ng tarafiga Koshi-Bunyakovskiy tengsizligini q6llaymiz:

$$|u_{ttt}| \leq M \left( \sqrt{\sum_{n=1}^{\infty} |\bar{\varphi}_k^{(5)}|^2} + \sqrt{\sum_{n=1}^{\infty} |\bar{\psi}_k^{(5)}|^2} + \sqrt{\sum_{n=1}^{\infty} |\bar{\eta}_k^{(4)}|^2} \right) \sqrt{\sum_{n=1}^{\infty} \frac{1}{k^2}} \leq \\ \leq M \left( \|\varphi^V\|_{L_2(0,p)} + \|\psi^V\|_{L_2(0,p)} + \|\eta^{IV}\|_{L_2(0,p)} \right) < \infty$$

(11) qatordan t bóyicha uch marta xosila olingan qatorning ham yaqinlashuvchiligi shunday kórsatiladi.

### Masala yechimining turgunligi

Quyidagi normalarni kiritamiz:

$$\|u(x,t)\|_{L_2[0,p]} = \left( \int_0^p |u(x,t)|^2 dx \right)^{\frac{1}{2}}, \quad \|u(x,t)\|_{C(\bar{\Omega})} = \max_{\bar{\Omega}} |u(x,t)|.$$

**2-teorema.** Mayli 1-teoremaning shartlari órinli bólsin. Unda 1 masalaning (11) yechimi uchun quyidagi baholashlar órinli bóladi:

$$\|u(x,t)\|_{L_2[0,p]} \leq C_4 \left[ \|\varphi\|_{L_2} + \|\psi\|_{L_2} + \|\eta\|_{L_2} \right],$$

$$\|u(x,t)\|_{C(\bar{\Omega})} \leq C_5 \left[ \|\varphi\|_{W_2^1} + \|\psi\|_{L_2} + \|\eta\|_{L_2} \right].$$

### Adabiyotlar róyxati:

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